

Derivatives of trigonometric functions:

a) If $f(\theta) = \sin^3(4\theta)$ find $f'(\theta)$.

$$\begin{aligned} &= [\sin(4\theta)]^3. \quad f'(\theta) = \\ &3 [\sin(4\theta)]^2 \cdot [\cos(4\theta)] \cdot 4 \\ &= 12 \sin^2(4\theta) \cdot \cos(4\theta) \end{aligned}$$

b) If $w = \ln(\tan 2x)$ find w' .

$$w' = \frac{1}{\tan 2x} \cdot \sec^2(2x) \cdot 2$$

c) If $s = e^{2t} \cos(3t)$ find $s'(t)$.

$$s'(t) = e^{2t} \cdot [-\sin(3t) \cdot 3] + \cos(3t) \cdot e^{2t} \cdot 2$$

d) If $g(x) = \frac{\sec(3x)}{\sqrt{x^2+7}}$ find $g'(x)$.

$$g'(x) = \sqrt{x^2+7} \cdot [\sec(3x) \cdot \tan(3x) \cdot 3] - \sec(3x) \cdot \frac{1}{2\sqrt{x^2+7}} \cdot 2x$$

$$(x^2+7)$$